NON-CLASSICAL BOUNDARY VALUE PROBLEMS AND MAXWELL'S EQUATIONS

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We consider boundary value problem (BVP) for an elliptic system of partial differential equations A(x, D)U = F of arbitrary order 2m on a domain $\Omega \subset \mathbb{R}^n$ with the smooth boundary $\mathscr{S} := \partial \Omega$ and a normal system of boundary conditions $\gamma_{\mathscr{S}}(B_j(x, D)U) = G_j$, $j = 0, \ldots, m-1$ on \mathscr{S} in the scale of Bessel potential $\mathbb{H}_p^s(\Omega)$ and Besov $\mathbb{B}_{p,p}^s(\mathscr{S})$ spaces, including the case of negative s < 0 (spaces of distributions). We define rigorously the traces $\gamma_{\mathscr{S}}U$ of solutions on the boundary \mathscr{S} , obtain the representation formulae for U and write conditions for the unique solvability in terms of boundary pseudodifferential equations on the boundary.

The obtained results are applied to an extension of distributions $G \in \mathbb{B}^s_{p,p}(\mathscr{C})$ from a subsurface $\mathscr{C} \subset \mathscr{S}$ into the space $\mathbb{R}^n_{\mathscr{C}} := \mathbb{R}^n \setminus \mathscr{C}$, slit by the hypersurface \mathscr{C} .

Another, more important, application is the regularization of the non-elliptic BVP for the Maxwell's system, which is reduced to an equivalent pair of elliptic BVPs.

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