Under Collatz conjecture the Collatz mapping has no an asymptotic mixing property (mod 3)

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Abstract

By using properties of Markov homogeneous chains and Banach measure in N, it is proved that a relative frequency of even numbers in the sequence of *n*-th coordinates of all Collatz sequences is equal to the number $\frac{2}{3} + \frac{(-1)^{n+1}}{3 \times 2^{n+1}}$. It is shown also that an analogous numerical characteristic for numbers of the form 3m + 1 is equal to the number $\frac{3}{5} + \frac{(-1)^{n+1}}{15 \times 2^{2n}}$. By using these formulas it is proved that under Collatz conjecture the Collatz mapping has no an asymptotic mixing property (mod 3). It is constructed also an example of a real-valued function on the cartesian product N^2 of the set of all natural numbers N such that an equality its repeated integrals (with respect to Banach measure in N) implies that Collatz conjecture fails.